

# Prediction and Optimization of Weld Bead Volume for the Submerged Arc Process — Part 2

*Analytic models were developed to establish a relationship between process parameters and weld bead quality*

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**ABSTRACT.** As a part of a study and analysis on the effects of process parameters on weld bead volume in submerged arc welding (SAW) of pipes, mathematical models were developed to relate the process parameters and the weld bead quality parameters. Further, the optimization of weld bead volume was carried out using the optimization module available in the *MATLAB* version 4.2b software package. The mathematical models thus developed for optimization are also helpful in predicting the weld bead quality parameters and in setting process parameters at optimum values to achieve the desirable weld bead quality at a relatively low cost with a high degree of repeatability and increased production rate. Total volume of the weld bead, an important bead parameter, was optimized (minimized), keeping the dimensions of the other important bead parameters as constraints, to obtain sound and superior quality welded pipes. Sensitivity analysis was also carried out to predict the direct and few interaction effects of important bead parameters on the total volume of the weld bead, and the results are presented in graphical form. The results of the sensitivity analysis are very useful in understanding the interdependence of various weld bead quality parameters in controlling the volume of the weld bead, to improve weld quality, to increase productivity with the

available welding facilities and to minimize the total welding cost.

## Introduction

Submerged arc welding is widely employed as one of the major fabrication processes in industry due to its inherent advantages of deep penetration, smooth bead and superior quality (Ref. 1). In SAW of pipes, engineers are often faced with the problems of relating the process variables to the weld bead quality and optimization of the bead parameters. Also, welding is done with the aim of achieving a sound joint at a low cost. But without optimization, it is impossible to achieve low-cost welding. The design and optimization process is iterative, requiring the repeated use of the same set of calculations (Refs. 2, 3). Until recently, cost and time-intensive trial and error methods were used to determine the optimum process parameters for a required bead quality. Since any welding process is a multi-objective problem (maximum

penetration, minimum reinforcement, minimum heat input, minimum width, minimum dilution, low cost, maximum production rate), the optimum solution is a compromise (Ref. 4). Selection of an appropriate weld bead parameter is also equally important because if the selected parameter is the one determined and controlled by most of the other important bead parameters, then the optimization of that parameter will obviously include all the other parameters. Total volume of the weld bead is one of those important bead parameters controlled by most of the other bead parameters. Hence, the total volume, if optimized (minimized), obviously minimizes most of the other bead quality parameters such as heat input, dilution, reinforcement, bead width and penetration. But for a sound and strong weld, bead penetration should be maximized. Hence, in optimizing the total volume of the weld bead, the penetration, included as a constraint, should be set at its maximum value.

Minimizing the size of the weld bead reduces the welding cost through 1) reduced consumption of consumables such as electrodes and flux; 2) reduced heat input and energy consumption and 3) increased welding productivity through a high welding speed. Because of these advantages, the total volume of the weld bead should be optimized, having other bead parameters as constraints, rather than optimizing all the bead parameters individually. The total volume of the weld bead is the area of the weld bead cross section multiplied by the length of the weld bead. To reduce the complexity of the problem, the length of the bead is assumed as unity, which simplifies the equation. Now the total vol-

## KEY WORDS

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**Table 3 — Comparison of Observed and Predicted Values of Conformity Test**

S. No.	Process parameters				Penetration, mm			Dilution, %			Total Volume, mm <sup>3</sup>		
	V Volts	F m/min	S m/min	N mm	Observed Value	Predicted Value	Error %	Observed Value	Predicted Value	Error %	Observed Value	Predicted Value	Error %
1	27	0.70	0.67	36	3.00	3.08	+2.60	36.48	35.45	+2.91	41.66	41.50	2.21
2	27	1.39	0.75	35	3.70	3.75	-1.33	46.23	44.98	+2.84	44.34	44.11	2.85
3	28	0.70	0.61	35	3.20	3.10	+3.20	39.17	38.05	+2.94	42.25	43.14	2.06
						Average	2.38			2.89			2.40

Error =

$$\% \text{ Error} = \frac{\text{Observed value} - \text{predicted value}}{\text{Predicted value}} \times 100$$

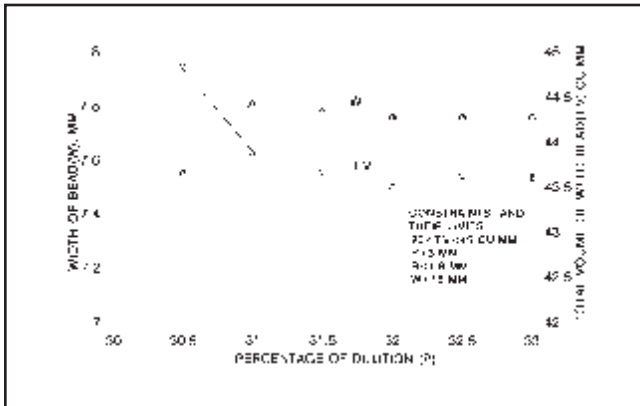


Fig. 9 — Direct effect of P on W and T.V.

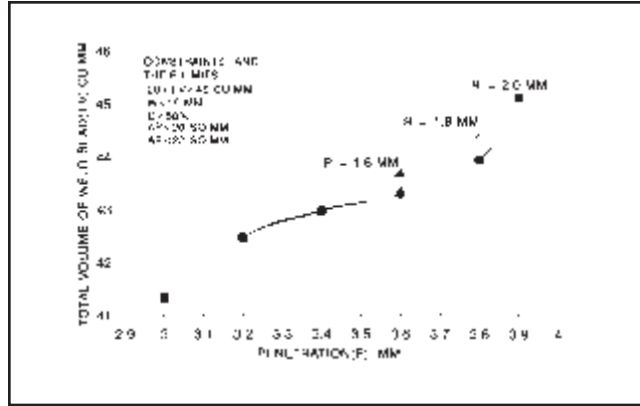


Fig. 10 — Interaction effect of P and R on T.V.

$0.03 \times X(1) \times X(3) + 0.04 \times X(1) \times X(4) - 0.01 \times X(2) \times X(3) - 0.01 \times X(2) \times X(4) + 0.08 \times X(3) \times X(4) + 3.0$ ; Penetration and its lower limit in mm.

$g(3) = 10.76 + 1.19 \times X(1) + 0.45 \times X(2) - 1.9 \times X(3) + 0.23 \times X(4) + 0.41 \times X(1)^2 - 0.17 \times X(2)^2 + 0.29 \times X(3)^2 + 0.12 \times X(4)^2 - 0.04 \times X(1) \times X(2) - 0.64 \times X(1) \times X(3) - 0.15 \times X(1) \times X(4) - 0.35 \times X(2) \times X(3) + 0.091 \times X(2) \times X(4) - 0.29 \times X(3) \times X(4) - 15.0$ ; Bead width and its upper limit in mm.

$g(4) = 47.27 + 0.74 \times X(1) + 2.51 \times X(2) - 0.25 \times X(3) - 2.23 \times X(4) - 1.31 \times X(1)^2 - 0.71 \times X(2)^2 - 1.31 \times X(3)^2 - 0.44 \times X(4)^2 - 0.09 \times X(1) \times X(2) - 0.3 \times X(1) \times X(3) - 0.31 \times X(1) \times X(4) + 0.43 \times X(2) \times X(3) - 0.90 \times X(2) \times X(4) + 0.17 \times X(3) \times X(4) - 50$ ; % Dilution and its upper limit.

$g(5) = 21.56 + 1.05 \times X(1) + 1.85 \times X(2) - 1.61 \times X(3) - 0.212 \times X(4) + 0.041 \times X(1)^2 + 0.29 \times X(2)^2 - 0.097 \times X(3)^2 + 0.15 \times X(4)^2 + 0.14 \times X(1) \times X(2) - 0.21 \times X(1) \times X(3) + 0.056 \times X(1) \times X(4) - 0.24 \times X(2) \times X(3) - 0.16 \times X(2) \times X(4) - 0.16 \times X(3) \times X(4) - 20$ ; Area of penetration and its upper limit.

$g(6) = 21.44 + 0.44 \times X(1) + 0.187 \times X(2) - 1.76 \times X(3) + 2.11 \times X(4) + 1.39 \times X(1)^2 -$

$0.39 \times X(2)^2 + 1.22 \times X(3)^2 + 0.62 \times X(4)^2 + 0.41 \times X(1) \times X(2) - 0.047 \times X(1) \times X(3) + 0.14 \times X(1) \times X(4) - 0.94 \times X(2) \times X(3) + 0.77 \times X(2) \times X(4) - 0.33 \times X(3) \times X(4) - 22$ ; Area of reinforcement and its upper limit.

$g(7) = f - 45$ ; upper limit of total weld bead volume is 45 mm<sup>3</sup>.

$g(8) = -f + 20$ ; lower limit of total weld bead volume is 20 mm<sup>3</sup>.

Step 2: Invoke an optimization routine (R-file)

$X_0 = [-1, -1, 1, 1]$  (guess of initial solution)

Options = [ ] (change in the default setting if any)

$V_{lb} = [-2, -2, -2, -2]$  (lower boundaries of the variables)

$V_{ub} = [2, 2, 2, 2]$  (upper boundaries of the variables)

$X = \text{Constr} ('f(X)' X_0; \text{options}; V_{lb}, V_{ub})$

Step 3: Running the M-file.

After running the M-file and retrieving the constraints, the optimum values of the process variables are the following:  
 X(1) = welding voltage (V) = 28 volts;  
 X(2) = wire feed rate (F) = 0.7 m/min;  
 X(3) = welding speed (S) = 0.64 m/min  
 X(4) = nozzle-to-plate distance (N) =

34.6 mm.

The results of optimization are given below.

T.V. = total volume of the weld bead = 41.33 mm<sup>3</sup>

R = reinforcement = 1.28 mm;  
 P = penetration = 3.07 mm;  
 W = width of the bead = 8.33 mm;  
 D = dilution of the bead = 38%;  
 AP = area of penetration = 18.13 mm<sup>2</sup>;  
 AR = area of reinforcement = 20.21 mm<sup>2</sup>.

**Sensitivity Analysis**

Sensitivity analysis, also known as the post optimality analysis, is the study of what happens to the value of the objective function if the limit of each of the constraints is changed from optimum value. Optimum solution for any function lies in a boundary or zone and, hence, it is not a single constant value (Ref. 10). This provides a flexibility in fixing the limits for the constraints. Also, for every value of each of the constraints there is a possibility for change in the value of the objective function as well as other constraints.

Therefore, it is very important to know the impact of relaxing the limits of each constraint on the value of the objective





